

BIOMEDICAL MATHEMATICS:

**Promising Directions in Imaging,
Therapy Planning, and Inverse Problems**

BIOMEDICAL MATHEMATICS:
**Promising Directions in Imaging,
Therapy Planning, and Inverse Problems**

Yair Censor, Ming Jiang, Ge Wang
Editors

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Preface

This book brings together 27 state-of-the-art, refereed and subsequently revised, research and review papers, by leading experts and practitioners in mathematical methods in biomedical imaging, in intensity-modulated radiation therapy (IMRT) and in optimization and inverse problems. The emphasis is on trying to discover relations and connections between these fields that will enhance progress in each of them. As this volume shows, applicable mathematical work in these fields goes hand-in-hand with real-world applications and the mutual “technology transfers” between them leads to further progress.

The topics covered here include mathematical aspects and practical problems in current major and emerging technologies in diagnostic and therapeutic medicine and biology research. The contributed work signifies the interdisciplinary cooperation between mathematicians and scientists from medical physics, engineering, clinical medicine, and biology that leads to mathematically based better solutions of practical problems in biomedical imaging and IMRT.

The Huangguoshu National Park of China, Guizhou, China, under the leadership of Mr. Degang Yuan, President of the Huangguoshu Tourism Group Company, LTD, recognizing the importance of the field and the need for interaction between theoreticians and practitioners, and desiring to create a high-profile cultural activity at the Huangguoshu National Park, provided us with a special grant to organize the “Huangguoshu International Interdisciplinary Conference on Biomedical Mathematics—Promising Directions in Imaging, Therapy Planning, and Inverse Problems.” The Conference took place during November 3–9, 2008, in the breathtaking Huangguoshu National Park of China.

The Conference was conducted under the scientific auspices of the Mathematical Center of the Ministry of Education of China at Peking University (PKU) in Beijing, China; the Center for Computational Mathematics and Scientific Computation (CCMSC) at the University of Haifa, Haifa, Israel; the School of Biomedical Engineering & Sciences at the Virginia Polytechnic Institute and State University, Virginia, USA; and the Guizhou University in Guiyang, Guizhou, China.

Experts from around the world were invited and participated. They came from Australia, Canada, Germany, Israel, Italy, Japan, Korea, P.R. China, Spain, Sweden, Switzerland, the United Kingdom, and the United States of America. Most of the papers in this volume originated from the lectures presented at the Conference, while others were written in the wake of discussions held during the Conference.

Preface

It is our pleasure to heartily thank Mr. Degang Yuan and the team of the Huangguoshu Tourism Group, Peking University, and Virginia Tech for their devoted and efficient work throughout all phases of the preparations for the conference. In particular we thank Dr. Lingyin Zhao, Zongmin (Tracy) Mao, Haifeng (Mountain) Tong, and Gang (Leo) Xie, from the the Huangguoshu Tourism Group; Prof. Tie Zhou, Dr. Caifang Wang, Dr. Xin Jiang, and Yuanzheng Si, Yu Zhou, Shengkun Shi, from Peking University (PKU); and Deepak Bharkhada, from Wake Forest University, for their cooperation and extraordinary support in organizing and conducting the Conference. Many thanks are due to the referees whose work enhanced the final versions of the papers which appear here. Last but not least, we thank the participants of the Conference and the authors who contributed their work to this volume. We gratefully acknowledge the help of Ms. Betsey Phelps, Managing Editor, Medical Physics Publishing, Madison, WI, USA, for her and her team's work on the production of this volume.

We hope that researchers in applied mathematics, medical physics, biomedical imaging, and intensity-modulated radiation therapy will find this book a useful tool in their current research and development efforts.

Yair Censor, Ming Jiang and Ge Wang
Haifa, Beijing, and Blacksburg, VA, respectively
January 31, 2010

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Real - time imaging for radiation therapy guidance Biomedical Mathematics : Promising Directions in Imaging , Therapy Planning , and Inverse Problems ed. L Xing. 2010. Assessment of two novel ventilatory surrogates for use in the delivery of gated/tracked radiotherapy for non-small cell lung cancer. Simon R. Hughes, James McClelland, +4 authors David Landau. Medicine. Radiotherapy and oncology : journal of the European Society for Therapeutic Radiology and Oncology. Search for IMRT inverse plans with piecewise constant fluence maps using compressed sensing techniques. Lei Zhu, Lei Xing. Mathematics, Medicine. Medical physics. 2009. VIEW 1 EXCERPT. quite interesting and promising. In Mueller-Bierl et al.'s paper, the authors investigated the magnetic field distribution and signal decay of high field strength functional MRI imaging. The static dipole model has been extended to a dynamic model to describe the same. The EIT and elasticity imaging in the following two contributions are inverse problems of partial differential equations. In EIT, electric currents are applied to the boundary of an object and the induced surface voltages are measured. The measured voltage data are then used to reconstruct the internal conductivity distribution of the object. Start by marking "Biomedical Mathematics: Promising Directions in Imaging, Therapy, Planning and Inverse Problems" as Want to Read: Want to Read saving as | Want to Read. Currently Reading. Read. Biomedical Mathematics by Yair Censor. Other editions. Want to Read saving as | Error rating book. Refresh and try again. Rate this book. Clear rating. 1 of 5 stars 2 of 5 stars 3 of 5 stars 4 of 5 stars 5 of 5 stars. Open Preview. See a Problem? We'd love your help. Let us know what's wrong with this preview of Biomedical Mathematics by Yair Censor. Problem: It's the wrong book It's the wrong edition Other Biomedical Mathematics: Promising Directions in Imaging, Therapy Planning and Inverse Problems This book brings together 27 state-of-the-art, refereed and subsequently revised, research and review papers, by leading experts and practitioners in mathematical methods in biomedical imaging, in intensity-modulated radiation therapy (IMRT) and in optimization and inverse problems. This book brings together 27 state-of-the-art, refereed and subsequently revised, research and review papers, by leading experts and practitioners in mathematical methods in biomedical imaging, in intensity-modulated radiation therapy (IMRT) and in optimization and inverse problems.